

Name: \_\_\_\_\_

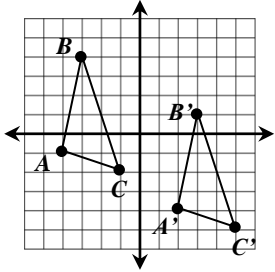
Date: \_\_\_\_\_

Topic: \_\_\_\_\_

Class: \_\_\_\_\_

Main Ideas/Questions	Notes/Examples
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## TRANSFORMATIONS



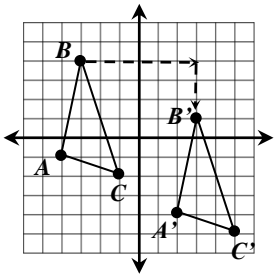
- A transformation is an operation that maps an original figure called the \_\_\_\_\_ onto a new figure called the \_\_\_\_\_.
- On the graph to the left, \_\_\_\_\_ is the preimage and \_\_\_\_\_ is the image. (' is read as "prime")
- A transformation can change the \_\_\_\_\_, \_\_\_\_\_, or \_\_\_\_\_ of a figure.

## RIGID MOTION



Examples of rigid motions:

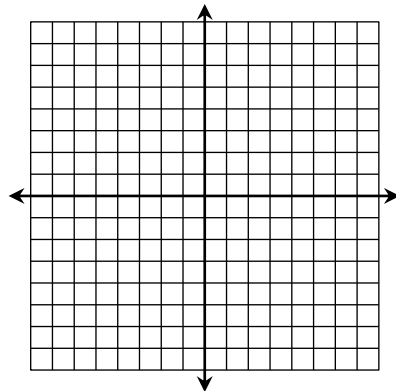
## TRANSLATION



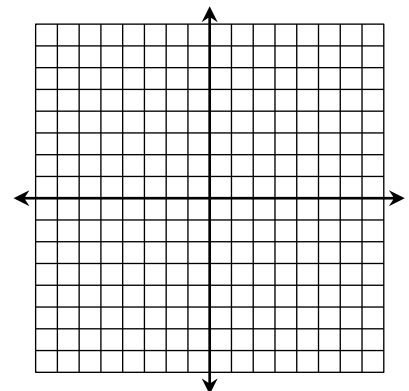
Coordinate Notation: \_\_\_\_\_  
 \_\_\_\_\_ represents the \_\_\_\_\_  
 \_\_\_\_\_ represents the \_\_\_\_\_

**Graph and label each figure and its image under the given translation. Identify the coordinates of the image.**

1. Rectangle  $QRST$  with vertices  $Q(-6, -1)$ ,  $R(-3, 1)$ ,  $S(1, -5)$ , and  $T(-2, -7)$ :  $(x, y) \rightarrow (x + 5, y + 7)$



2. Triangle  $CDE$  with vertices  $C(2, -1)$ ,  $D(7, -4)$ , and  $E(4, -6)$ :  $(x, y) \rightarrow (x - 3, y + 8)$



$Q'$ : \_\_\_\_\_

$S'$ : \_\_\_\_\_

$C'$ : \_\_\_\_\_

$E'$ : \_\_\_\_\_

$R'$ : \_\_\_\_\_

$T'$ : \_\_\_\_\_

$D'$ : \_\_\_\_\_

\_\_\_\_\_

Name: \_\_\_\_\_

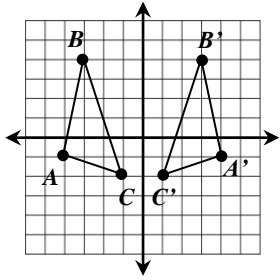
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Main Ideas/Questions	Notes/Examples
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# REFLECTION



- A \_\_\_\_\_ over a line called the \_\_\_\_\_.
- Each point and its image are the \_\_\_\_\_ from the line of reflection.
- A reflection is also an example of a \_\_\_\_\_.

**Common lines of reflection:**

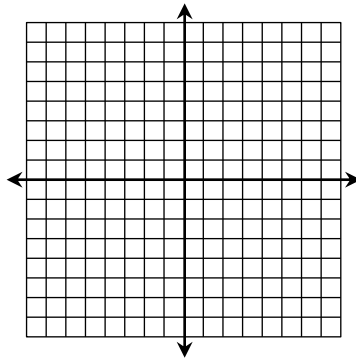
- \_\_\_\_\_ - \_\_\_\_\_ or \_\_\_\_\_ - \_\_\_\_\_
- Vertical or horizontal lines in the form \_\_\_\_\_ or \_\_\_\_\_
- Diagonal lines, for example, \_\_\_\_\_ or \_\_\_\_\_

Reflecting in

## THE X-AXIS AND Y-AXIS

**Graph and label each figure and its image under a reflection in the given line. Give the coordinates of the image.**

1. Triangle *ABC* with vertices  $A(-4, 2)$ ,  $B(4, 7)$ , and  $C(5, 1)$ : **x-axis**

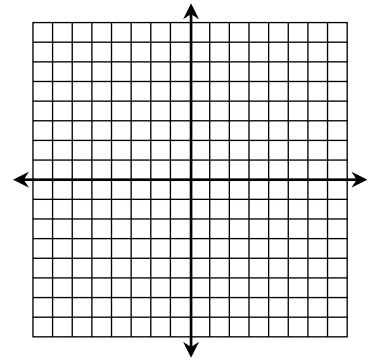


$A'$ : \_\_\_\_\_

$C'$ : \_\_\_\_\_

$B'$ : \_\_\_\_\_

2. Rectangle *PQRS* with vertices  $P(1, 2)$ ,  $Q(2, 5)$ ,  $R(8, 3)$ , and  $S(7, 0)$ : **y-axis**



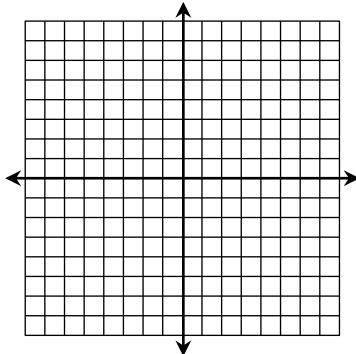
$P'$ : \_\_\_\_\_

$R'$ : \_\_\_\_\_

$Q'$ : \_\_\_\_\_

$S'$ : \_\_\_\_\_

3. Trapezoid *FGHI* with vertices  $F(-5, -2)$ ,  $G(-2, -2)$ ,  $H(0, -6)$ , and  $I(-8, -6)$ : **y-axis**



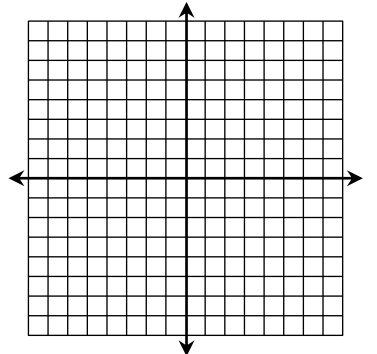
$F'$ : \_\_\_\_\_

$H'$ : \_\_\_\_\_

$G'$ : \_\_\_\_\_

$I'$ : \_\_\_\_\_

4. Rhombus *WXYZ* with vertices  $W(-2, -4)$ ,  $X(1, -2)$ ,  $Y(4, -4)$ , and  $Z(1, -6)$ : **x-axis**

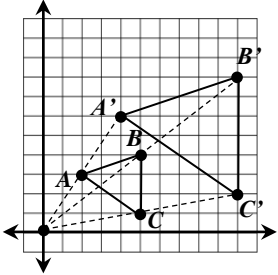


$W'$ : \_\_\_\_\_

$Y'$ : \_\_\_\_\_

$X'$ : \_\_\_\_\_

$Z'$ : \_\_\_\_\_

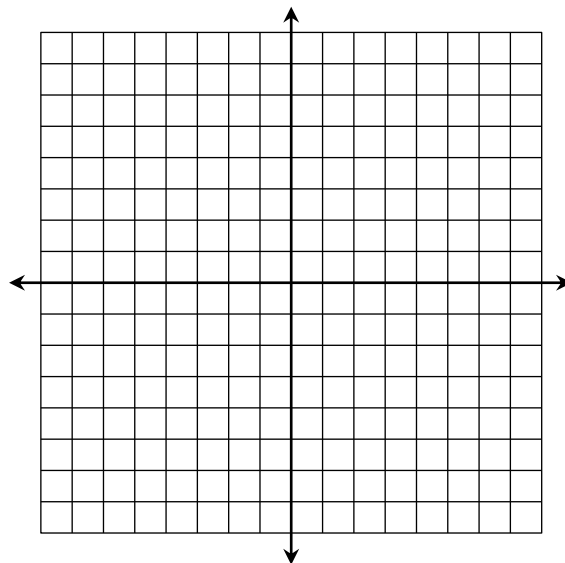
Main Ideas/Questions	Notes/Examples
<h2 style="text-align: center;">DILATION</h2> 	<ul style="list-style-type: none"> <li>A dilation is a _____ of a figure with respect to a fixed point, called the _____.</li> <li>A dilation is an example of a _____ in that it does not preserve congruency.</li> <li>A dilation produces _____.</li> <li>All corresponding angles are congruent, and all corresponding sides are proportional.</li> </ul>
<h2 style="text-align: center;">SCALE FACTOR</h2>	<ul style="list-style-type: none"> <li>The <b>scale factor</b> indicates how much the figure will enlarge or reduce.</li> <li>Variable for scale factor: _____ <ul style="list-style-type: none"> <li>➤ When _____, the dilation is an _____.</li> <li>➤ When _____, the dilation is a _____.</li> </ul> </li> </ul>
<h2 style="text-align: center;">DILATION RULE</h2> <p style="text-align: center;">(origin as center)</p>	<p>If <math>P(x, y)</math> is the preimage of a point, then its image after a dilation centered at the origin <math>(0, 0)</math> with scale factor <math>k</math> will follow the rule:</p>

**Graph and label each figure and its image under the sequence of transformations. Give the coordinates of the image.**

1. Triangle  $XYZ$  with vertices  $X(-3, 7)$ ,  $Y(-2, 1)$ , and  $Z(-5, 2)$ :

a) reflection in the  $x$ -axis

b) translation along the rule  $(x, y) \rightarrow (x + 9, y + 2)$



$X'(\underline{\quad}, \underline{\quad})$

$Y'(\underline{\quad}, \underline{\quad})$

$Z'(\underline{\quad}, \underline{\quad})$

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**Main Ideas/Questions**

## TRANSFORMATIONS

**Notes/Examples**

- A transformation is an operation that maps an original figure called the pre-image onto a new figure called the image.
- On the graph to the left,  $\triangle ABC$  is the pre-image and  $\triangle A'B'C'$  is the image. (' is read as "prime")
- A transformation can change the position, orientation or size of a figure.

**RIGID MOTION**

When a transformation preserves the size and shape of a figure. All corresponding sides + angles of the pre-image + image are congruent.  
 Examples of rigid motions: translations, reflections, rotations

**TRANSLATION**

To vertically and/or horizontally SLIDE a figure

Coordinate Notation:  $(x, y) \rightarrow (x+h, y+k)$

h represents the horizontal shift

k represents the vertical shift

Graph and label each figure and its image under the given translation. Identify the coordinates of the image.

1. Rectangle  $QRST$  with vertices  $Q(-6, -1)$ ,  $R(-3, 1)$ ,  $S(1, -5)$ , and  $T(-2, -7)$ :  $(x, y) \rightarrow (x+5, y+7)$

2. Triangle  $CDE$  with vertices  $C(2, -1)$ ,  $D(7, -4)$ , and  $E(4, -6)$ :  $(x, y) \rightarrow (x-3, y+8)$

$Q': (-1, 6)$   
 $R': (2, 8)$

$S': (6, 2)$   
 $T': (3, 0)$

$C': (-1, 7)$   
 $D': (4, 4)$

$E': (1, 2)$

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**Main Ideas/Questions**

# REFLECTION

**Notes/Examples**

- A FLIP over a line called the line of reflection.
- Each point its image are the same distance from the line of reflection.
- A reflection is also an example of a rigid motion.

**Common lines of reflection:**

- x - axis or y - axis
- Vertical or horizontal lines in the form x = # or y = #
- Diagonal lines, for example, y = x or y = -x

*Reflecting in*  
**THE X-AXIS  
AND Y-AXIS**

**Graph and label each figure and its image under a reflection in the given line. Give the coordinates of the image.**

1. Triangle  $ABC$  with vertices  $A(-4, 2)$ ,  $B(4, 7)$ , and  $C(5, 1)$ : x-axis

2. Rectangle  $PQRS$  with vertices  $P(1, 2)$ ,  $Q(2, 5)$ ,  $R(8, 3)$ , and  $S(7, 0)$ : y-axis

$A': (-4, -2)$        $C': (5, -1)$

$P': (-1, 2)$        $R': (-8, 3)$

$B': (4, -7)$

$Q': (-2, 5)$        $S': (-7, 0)$

3. Trapezoid  $FGHI$  with vertices  $F(-5, -2)$ ,  $G(-2, -2)$ ,  $H(0, -6)$ , and  $I(-8, -6)$ : y-axis

4. Rhombus  $WXYZ$  with vertices  $W(-2, -4)$ ,  $X(1, -2)$ ,  $Y(4, -4)$ , and  $Z(1, -6)$ : x-axis

$F': (5, -2)$        $H': (0, -6)$

$W': (-2, 4)$        $Y': (4, 4)$

$G': (2, -2)$        $I': (-8, -6)$

$X': (1, 2)$        $Z': (1, 6)$

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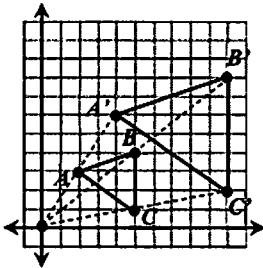
Topic:

Class:

### Main Ideas/Questions

### Notes/Examples

## DILATION



- A dilation is a enlargement or reduction of a figure with respect to a fixed point, called the Center of dilation.
- A dilation is an example of a nonrigid motion in that it does not preserve congruency.
- A dilation produces similar figures.
- All corresponding angles are congruent, and all corresponding sides are proportional.

## SCALE FACTOR

- The **scale factor** indicates how much the figure will enlarge or reduce.
- Variable for scale factor:  $k$ 
  - When  $k > 1$ , the dilation is an enlargement.
  - When  $k < 1$ , the dilation is an reduction.

## DILATION RULE

(origin as center)

If  $P(x, y)$  is the preimage of a point, then its image after a dilation centered at the origin  $(0, 0)$  with scale factor  $k$  will follow the rule:

$$(x, y) \rightarrow (kx, ky)$$

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Main Ideas/Questions

Notes/Examples

## SEQUENCES OF Transformations

When two or more transformations are combined to form a transformation.

Graph and label each figure and its image under the sequence of transformations. Give the coordinates of the image.

- Triangle  $XYZ$  with vertices  $X(-3, 7)$ ,  $Y(-2, 1)$ , and  $Z(-5, 2)$ :
  - reflection in the  $x$ -axis
  - translation along the rule  $(x, y) \rightarrow (x + 9, y + 2)$

$X'(6, -5)$   
 $Y'(7, 1)$   
 $Z'(4, 0)$

